

$$c) I_L = 300A \Rightarrow I_A = 300 - 5 = 295A$$

$$E_A = 250 - 0.06 \times 295 = 232.3V$$

$$\frac{1200}{n_2} = \frac{250}{232.3} \Rightarrow n_2 = 1115 \text{ rpm}$$

$$I_A = 0 \text{ (no-load)} \quad | \quad 1200$$

$$I_A = 100 \quad | \quad 1173$$

$$I_A = 200 \quad | \quad 1144$$

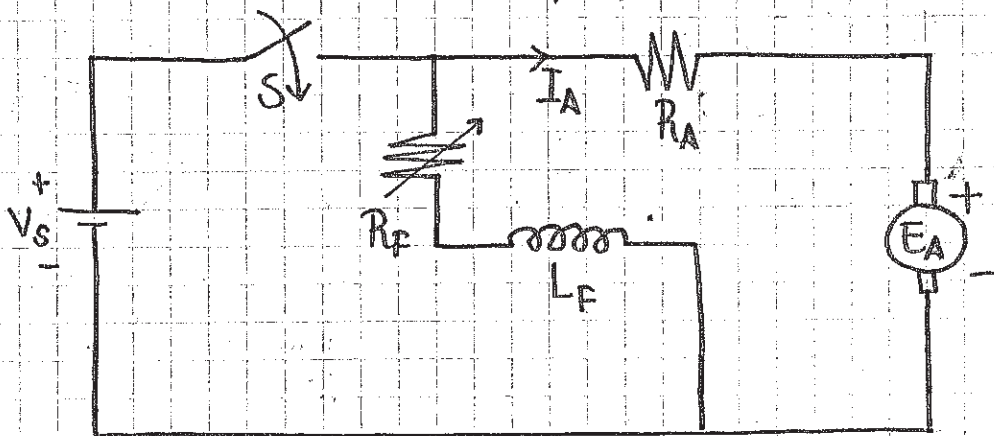
$$I_A = 300 \quad | \quad 1115$$

$n \text{ (rpm)}$

6 Nisan Çarşamba 2011

Starters in DC Motors:

The starting current of DC motors is very high and should be limited to obtain a proper operation.



Switch S is closed at $t=0$

$$V_s = R_A I_A + E_A \Rightarrow I_A = \frac{V_s - E_A}{R_A}$$

$$E = K\phi\omega \Rightarrow I_A = \frac{V_s - K\phi\omega}{R_A}$$

At starting $n=0$ or $\omega=0 \Rightarrow E_A(t=0^+) = 0$

$$** \left\{ I_A = \frac{V_s}{R} \right\} \Rightarrow I_A \text{ (starting)}$$

Example: For a shunt DC Motor with armature resistance of 0.2Ω find the starting current.

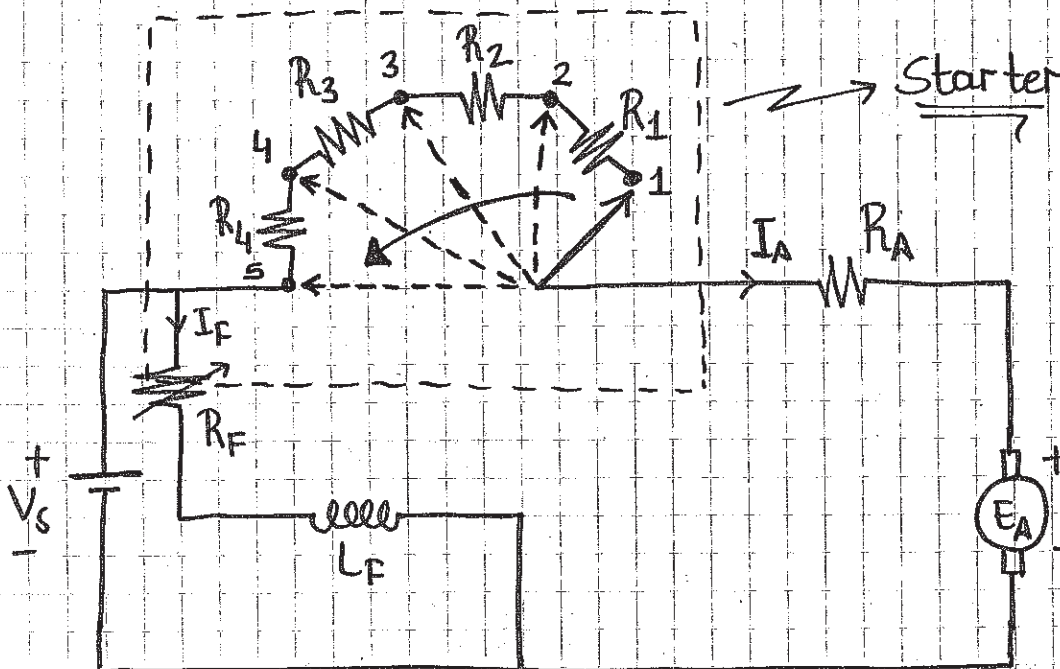
The motor is supply from a 200Vdc source

$$\left. \begin{array}{l} V_s = 200 \\ R_A = 0.2 \end{array} \right\} I_A(\text{starting}) = \frac{200}{0.2} = \underline{1000A}$$

Starters \Rightarrow DC motorlarda motorun başlangıç akımı çok yüksek olduğu için, bu durumun önüne geçmeye yarayan cihazlardır...

ex: DC motorun nominal ^{akım} değeri $\Rightarrow 50A$ iken
starting akım değeri $\Rightarrow 1000A$

Starting akım değerini düşürmeye yarayan \Rightarrow starters



$$\text{At } t=0 \rightarrow I_A = \frac{V_s - K\phi\omega}{R_A + [R_1 + R_2 + R_3 + R_4]}$$

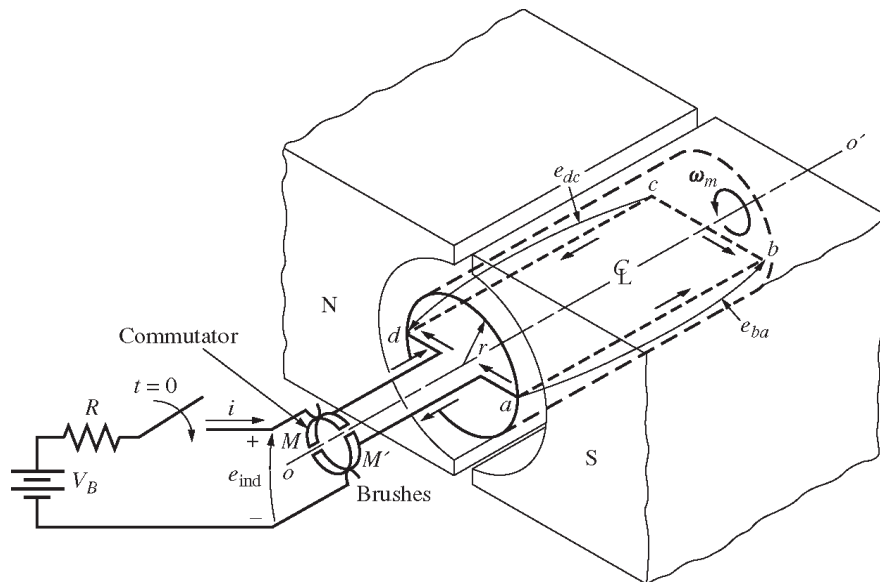
$$\omega(t=0) = 0 \rightarrow I_A(t=0) = \frac{V_s}{R_A + R_1 + R_2 + R_3 + R_4}$$

Chapter 8: DC Motors

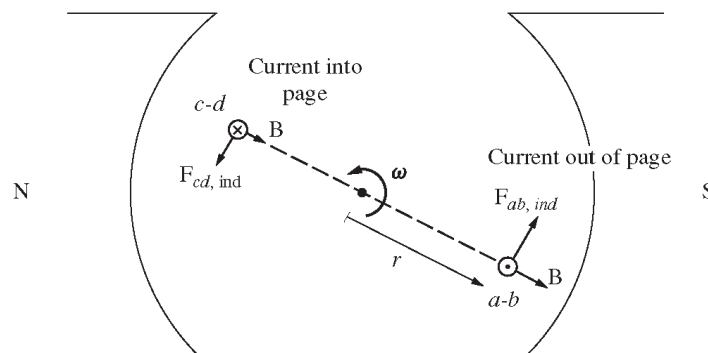
8-1. The following information is given about the simple rotating loop shown in Figure 8-6:

$$\begin{array}{ll}
 B = 0.4 \text{ T} & V_B = 48 \text{ V} \\
 l = 0.5 \text{ m} & R = 0.4 \ \Omega \\
 r = 0.25 \text{ m} & \omega = 500 \text{ rad/s}
 \end{array}$$

- Is this machine operating as a motor or a generator? Explain.
- What is the current i flowing into or out of the machine? What is the power flowing into or out of the machine?
- If the speed of the rotor were changed to 550 rad/s, what would happen to the current flow into or out of the machine?
- If the speed of the rotor were changed to 450 rad/s, what would happen to the current flow into or out of the machine?



(a)



(b)

SOLUTION

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(a) If the speed of rotation ω of the shaft is 500 rad/s, then the voltage induced in the rotating loop will be

$$e_{\text{ind}} = 2rB\omega$$

$$e_{\text{ind}} = 2(0.25 \text{ m})(0.5 \text{ m})(0.4 \text{ T})(500 \text{ rad/s}) = 50 \text{ V}$$

Since the external battery voltage is only 48 V, this machine is operating as a *generator*, charging the battery.

(b) The current flowing out of the machine is approximately

$$i = \frac{e_{\text{ind}} - V_B}{R} = \left(\frac{50 \text{ V} - 48 \text{ V}}{0.4 \Omega} \right) = 5.0 \text{ A}$$

(Note that this value is the current flowing while the loop is under the pole faces. When the loop goes beyond the pole faces, e_{ind} will momentarily fall to 0 V, and the current flow will momentarily reverse. Therefore, the *average* current flow over a complete cycle will be somewhat less than 5.0 A.)

(c) If the speed of the rotor were increased to 550 rad/s, the induced voltage of the loop would increase to

$$e_{\text{ind}} = 2rB\omega$$

$$e_{\text{ind}} = 2(0.25 \text{ m})(0.5 \text{ m})(0.4 \text{ T})(550 \text{ rad/s}) = 55 \text{ V}$$

and the current flow out of the machine will increase to

$$i = \frac{e_{\text{ind}} - V_B}{R} = \left(\frac{55 \text{ V} - 48 \text{ V}}{0.4 \Omega} \right) = 17.5 \text{ A}$$

(d) If the speed of the rotor were decreased to 450 rad/s, the induced voltage of the loop would fall to

$$e_{\text{ind}} = 2rB\omega$$

$$e_{\text{ind}} = 2(0.25 \text{ m})(0.5 \text{ m})(0.4 \text{ T})(450 \text{ rad/s}) = 45 \text{ V}$$

Here, e_{ind} is less than V_B , so current flows into the loop and the machine is acting as a motor. The current flow into the machine would be

$$i = \frac{V_B - e_{\text{ind}}}{R} = \left(\frac{48 \text{ V} - 45 \text{ V}}{0.4 \Omega} \right) = 7.5 \text{ A}$$

8-2. The power converted from one form to another within a dc motor was given by

$$P_{\text{conv}} = E_A I_A = \tau_{\text{ind}} \omega_m$$

Use the equations for E_A and τ_{ind} [Equations (8-30) and (8-31)] to prove that $E_A I_A = \tau_{\text{ind}} \omega_m$; that is, prove that the electric power disappearing at the point of power conversion is exactly equal to the mechanical power appearing at that point.

SOLUTION

$$P_{\text{conv}} = E_A I_A$$

Substituting Equation (8-30) for E_A

$$P_{\text{conv}} = (K \phi \omega) I_A$$

$$P_{\text{conv}} = (K \phi I_A) \omega$$

But from Equation (8-31), $\tau_{\text{ind}} = K \phi I_A$, so

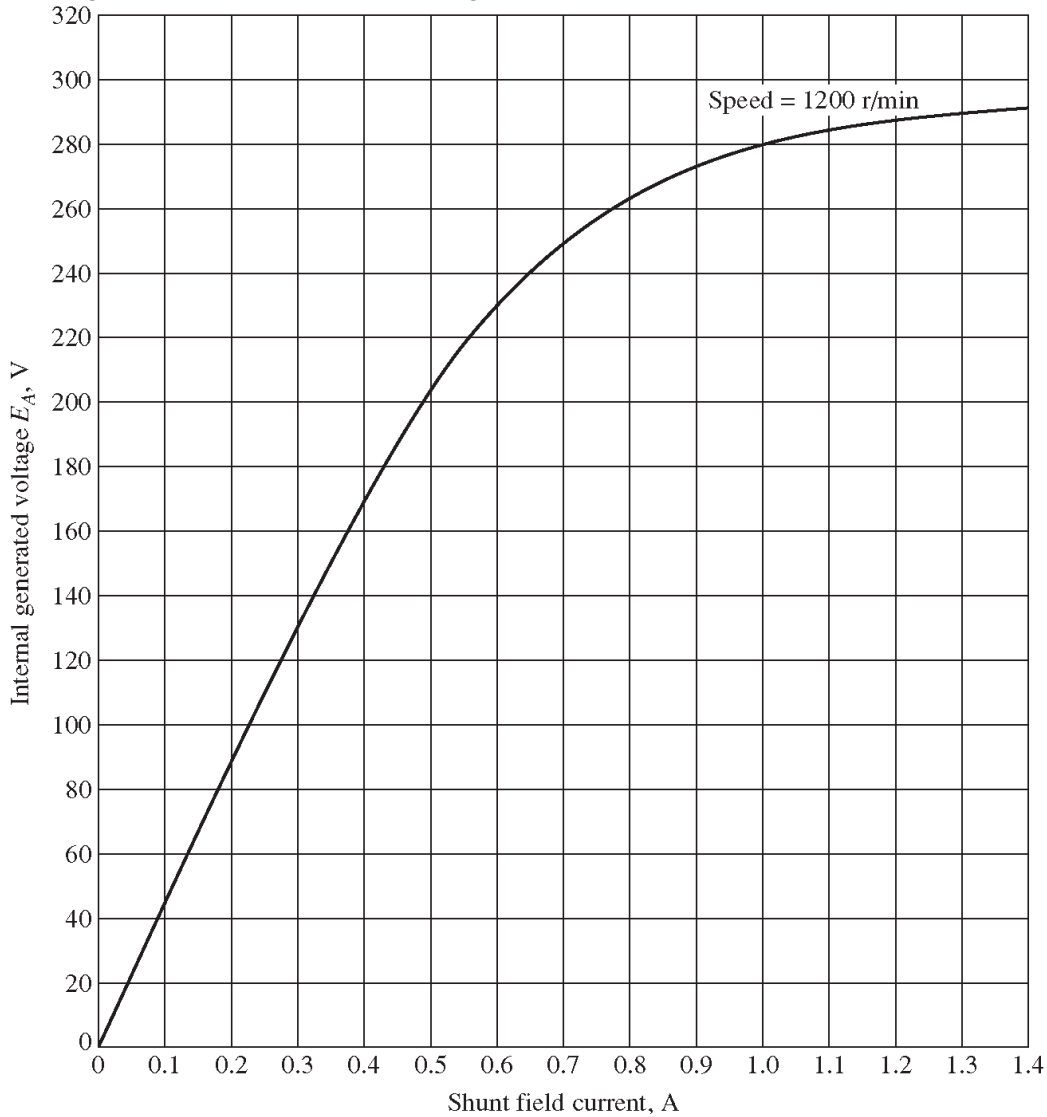
$$P_{\text{conv}} = \tau_{\text{ind}} \omega$$

Problems 8-3 to 8-14 refer to the following dc motor:

$P_{\text{rated}} = 30 \text{ hp}$	$I_{L,\text{rated}} = 110 \text{ A}$
$V_T = 240 \text{ V}$	$N_F = 2700 \text{ turns per pole}$
$n_{\text{rated}} = 1200 \text{ r/min}$	$N_{SE} = 12 \text{ turns per pole}$
$R_A = 0.19 \Omega$	$R_F = 75 \Omega$
$R_S = 0.02 \Omega$	$R_{\text{adj}} = 100 \text{ to } 400 \Omega$

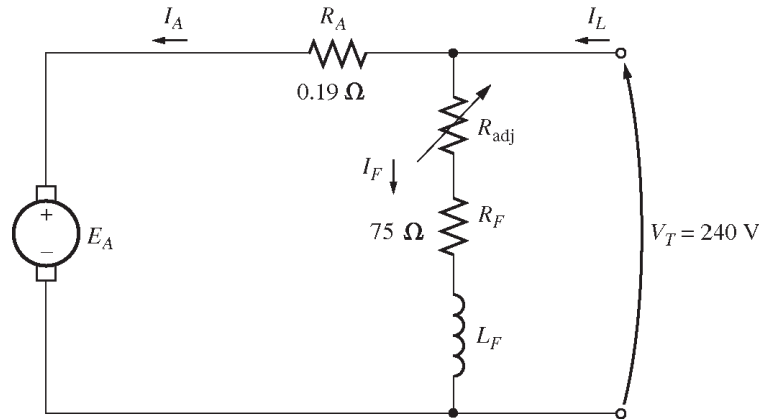
Rotational losses = 3550 W at full load

Magnetization curve as shown in Figure P8-1



In Problems 8-3 through 8-9, assume that the motor described above can be connected in shunt. The equivalent circuit of the shunt motor is shown in Figure P8-2.

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- 8-3.** If the resistor R_{adj} is adjusted to 175Ω what is the rotational speed of the motor at no-load conditions?

SOLUTION At no-load conditions, $E_A = V_T = 240 \text{ V}$. The field current is given by

$$I_F = \frac{V_T}{R_{adj} + R_F} = \frac{240 \text{ V}}{175 \Omega + 75 \Omega} = \frac{240 \text{ V}}{250 \Omega} = 0.96 \text{ A}$$

From Figure P8-1, this field current would produce an internal generated voltage E_{Ao} of 277 V at a speed n_o of 1200 r/min . Therefore, the speed n with a voltage of 240 V would be

$$\frac{E_A}{E_{Ao}} = \frac{n}{n_o}$$

$$n = \left(\frac{E_A}{E_{Ao}} \right) n_o = \left(\frac{240 \text{ V}}{277 \text{ V}} \right) (1200 \text{ r/min}) = 1040 \text{ r/min}$$

- 8-4.** Assuming no armature reaction, what is the speed of the motor at full load? What is the speed regulation of the motor?

SOLUTION At full load, the armature current is

$$I_A = I_L - I_F = 110 \text{ A} - 0.96 \text{ A} = 109 \text{ A}$$

The internal generated voltage E_A is

$$E_A = V_T - I_A R_A = 240 \text{ V} - (109 \text{ A})(0.19 \Omega) = 219.3 \text{ V}$$

The field current is the same as before, and there is no armature reaction, so E_{Ao} is still 277 V at a speed n_o of 1200 r/min . Therefore,

$$n = \left(\frac{E_A}{E_{Ao}} \right) n_o = \left(\frac{219.3 \text{ V}}{277 \text{ V}} \right) (1200 \text{ r/min}) = 950 \text{ r/min}$$

The speed regulation is

$$\text{SR} = \frac{n_{nl} - n_{fl}}{n_{fl}} \times 100\% = \frac{1040 \text{ r/min} - 950 \text{ r/min}}{950 \text{ r/min}} \times 100\% = 9.5\%$$

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- 8-5.** If the motor is operating at full load and if its variable resistance R_{adj} is increased to 250Ω , what is the new speed of the motor? Compare the full-load speed of the motor with $R_{\text{adj}} = 175 \Omega$ to the full-load speed with $R_{\text{adj}} = 250 \Omega$. (Assume no armature reaction, as in the previous problem.)

SOLUTION If R_{adj} is set to 250Ω , the field current is now

$$I_F = \frac{V_T}{R_{\text{adj}} + R_F} = \frac{240 \text{ V}}{250 \Omega + 75 \Omega} = \frac{240 \text{ V}}{325 \Omega} = 0.739 \text{ A}$$

Since the motor is still at full load, E_A is still 219.3 V . From the magnetization curve (Figure P8-1), this current would produce a voltage E_{A_o} of 256 V at a speed n_o of 1200 r/min . Therefore,

$$n = \left(\frac{E_A}{E_{A_o}} \right) n_o = \left(\frac{219.3 \text{ V}}{256 \text{ V}} \right) (1200 \text{ r/min}) = 1028 \text{ r/min}$$

Note that R_{adj} has increased, and as a result the speed of the motor n increased.

- 8-6.** Assume that the motor is operating at full load and that the variable resistor R_{adj} is again 175Ω . If the armature reaction is $1200 \text{ A}\cdot\text{turns}$ at full load, what is the speed of the motor? How does it compare to the result for Problem 8-5?

SOLUTION The field current is again 0.96 A , and the motor is again at full load conditions. However, this time there is an armature reaction of $1200 \text{ A}\cdot\text{turns}$, and the *effective* field current is

$$I_F^* = I_F - \frac{\text{AR}}{N_F} = 0.96 \text{ A} - \frac{1200 \text{ A}\cdot\text{turns}}{2700 \text{ turns}} = 0.516 \text{ A}$$

From Figure P8-1, this field current would produce an internal generated voltage E_{A_o} of 210 V at a speed n_o of 1200 r/min . The actual internal generated voltage E_A at these conditions is

$$E_A = V_T - I_A R_A = 240 \text{ V} - (109 \text{ A})(0.19 \Omega) = 219.3 \text{ V}$$

Therefore, the speed n with a voltage of 240 V would be

$$n = \left(\frac{E_A}{E_{A_o}} \right) n_o = \left(\frac{219.3 \text{ V}}{210 \text{ V}} \right) (1200 \text{ r/min}) = 1253 \text{ r/min}$$

If all other conditions are the same, the motor with armature reaction runs at a higher speed than the motor without armature reaction.

- 8-7.** If R_{adj} can be adjusted from 100 to 400Ω , what are the maximum and minimum no-load speeds possible with this motor?

SOLUTION The minimum speed will occur when $R_{\text{adj}} = 100 \Omega$, and the maximum speed will occur when $R_{\text{adj}} = 400 \Omega$. The field current when $R_{\text{adj}} = 100 \Omega$ is:

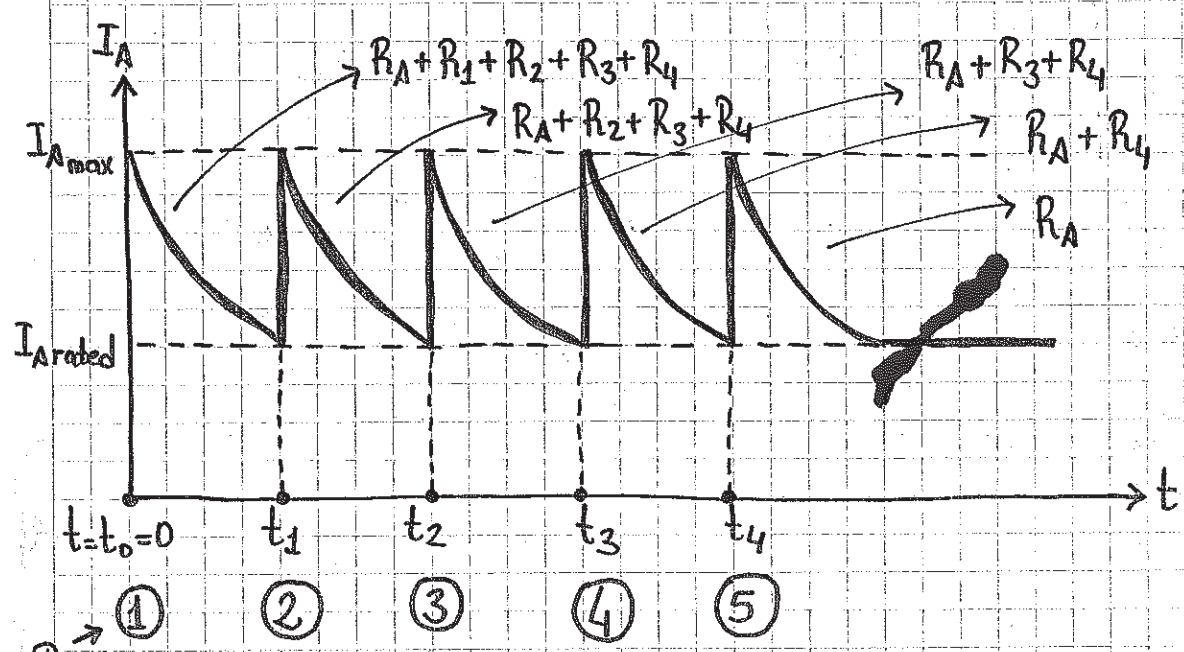
$$I_F = \frac{V_T}{R_{\text{adj}} + R_F} = \frac{240 \text{ V}}{100 \Omega + 75 \Omega} = \frac{240 \text{ V}}{175 \Omega} = 1.37 \text{ A}$$

From Figure P8-1, this field current would produce an internal generated voltage E_{A_o} of 289 V at a speed n_o of 1200 r/min . Therefore, the speed n with a voltage of 240 V would be

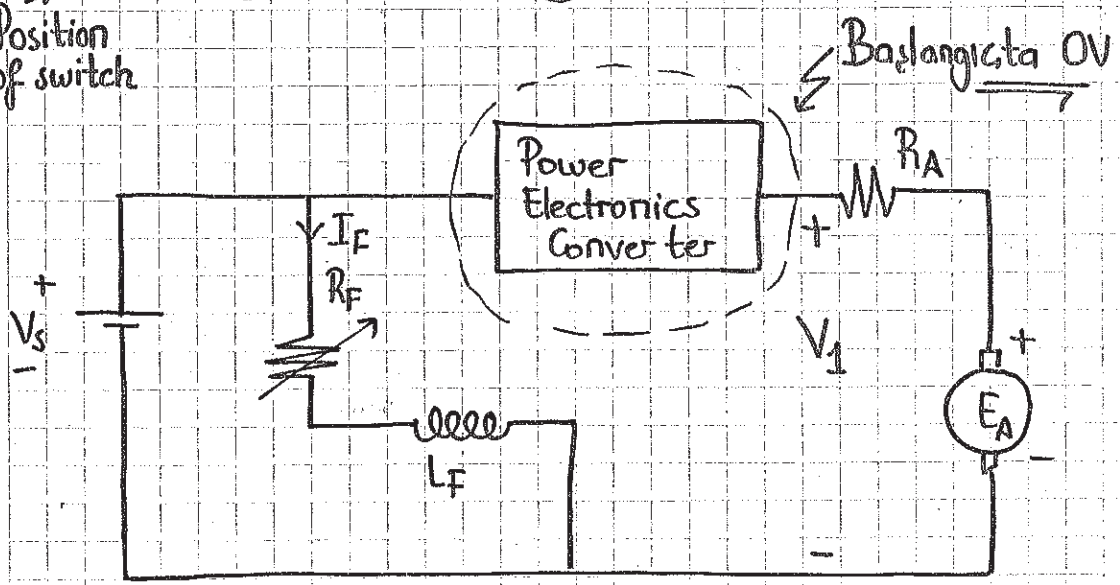
94

$\omega \uparrow \Rightarrow E_A \uparrow \Rightarrow I_A \downarrow$
 with increasing of motor speed the armature current decreases

$$I_A = \frac{V_s - K\phi\omega}{\text{-----}}$$



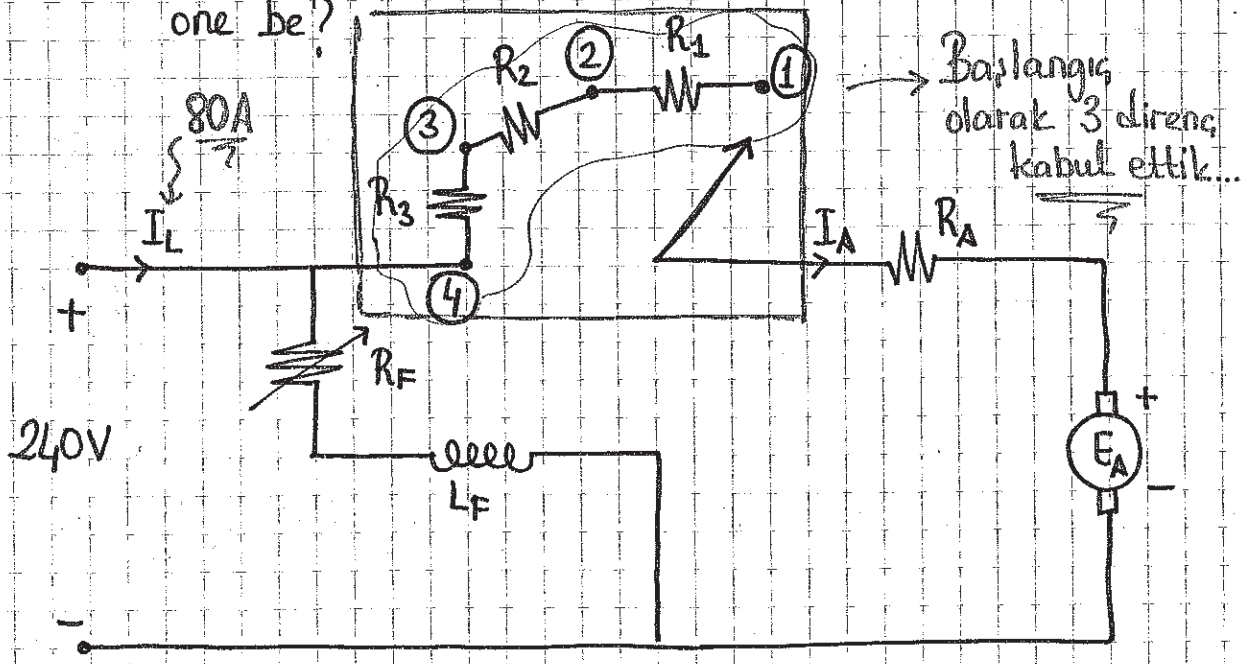
Position of switch



V_1 (voltage applied to motor) is adjusted using a converter.
 V_1 is increased from zero up to voltage rating of motor.

- 4/5 }
 Soru }
 Vize için }
 1 - ...
 2 - DC Machine (1 yada 2 soru)
 3 - Tanım
 4 - Trafo

Example: An automatic starter circuit is to be designed for a shunt motor at 20hp, 240V and 80A. The armature resistance of the motor is 0.12Ω and the shunt field resistance is 40Ω . The motor is to start with no more than 250 percent of its rated armature current, and as soon as the current falls to rated value, a starting resistor stage is be cut out. How many stages of starting resistance are needed and how big should each one be?



$R_A = 0.12\Omega$
 $R_F = 40\Omega$

$V_T = E_A + I_A R_A$

$V_T = K\phi\omega + I_A R_A$

$I_A = \frac{V_T - K\phi\omega}{R_A}$

$$I_A(t=0) = \frac{V_T - 0}{R_A}$$

$$I_A = \frac{V_T - E_A}{R_A + \sum R_{start}}$$

Without starter

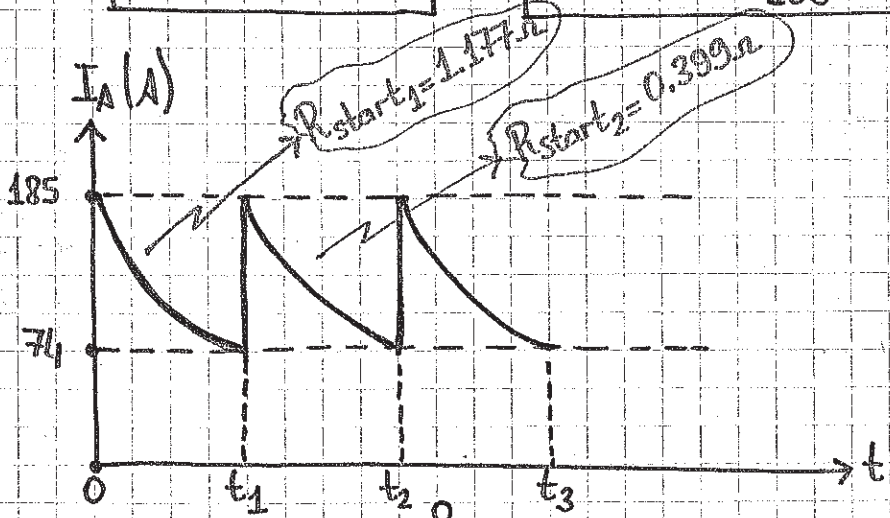
$$I_A(t=0) = \frac{240}{0.12} = \underline{\underline{2000A}}$$

$$80 = I_L = I_A + I_F = I_A + \frac{V_T}{R_F} = I_A + \frac{240}{40} = \underline{\underline{I_A + 6}}$$

$$I_A = 80 - 6 = 74A$$

$$\Rightarrow I_{A \text{ rated}} = 74A$$

$$I_{A \text{ max}} = \frac{250}{100} \times 74 = 185A$$



Motor hızlandıkça
 $E_A \uparrow$
 $E_A \uparrow$ aradaki fark azalır
 akım \downarrow
 $E_{A \text{ min}}, R_{\text{max}}$

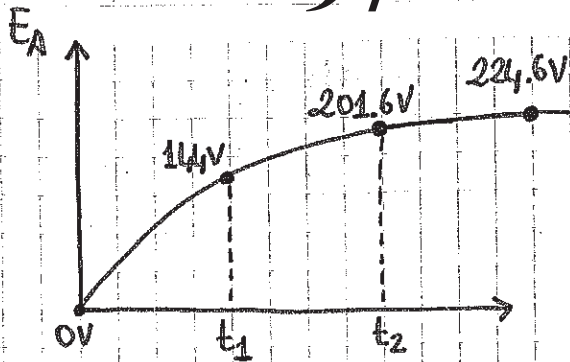
$$185 = \frac{240 - \overbrace{E_A(t=0)}^0}{R_A + R_{start1}} = \frac{240}{\underbrace{R_A}_{0.12\Omega} + R_{start1}} \Rightarrow R_{start1} = 1.177\Omega$$

$\Rightarrow R_{start1} = 1.177\Omega$
 \swarrow toplam seri direnç

$$185 = \frac{240 - E_A(t_1)}{R_A + R_{start2}} \Rightarrow \text{1. direnç devre dışı bırakıldı, geriye 2 direnç kaldı...}$$

$$E_A(t=t_1) = V_T - (R_A + 1.177) \times 74 = 114V$$

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$$I_A = \frac{V_T - 114}{R_A + R_{start2}}$$

$$I_A = \frac{240 - 114}{0.12 + R_{start2}} = 185 \text{ A}$$

$$R_{start2} = \underline{\underline{0.399 \Omega}}$$

$$\begin{aligned} \text{At } t_2 : E_A(t=t_2) &= V_T - I_{A \text{ rated}} (R_A + R_{start2}) \\ &= 240 - 74 (0.12 + 0.399) = 201.6 \text{ V} \end{aligned}$$

$$I_A = \frac{V_T - 201.6}{R_A + R_{start3}} \Rightarrow 185 = \frac{240 - 201.6}{0.12 + R_{start3}} \Rightarrow R_{start3} = \underline{\underline{0.088 \Omega}}$$

$$\begin{aligned} E_A(t=t_3) &= V_T - I_{A \text{ rated}} (R_A + R_{start3}) \\ &= 240 - 74 (0.12 + 0.088) = 224.6 \text{ V} \end{aligned}$$

$$I_A = \frac{V_T - 224.6}{R_A} = 128.3 < 185 \text{ A} \Rightarrow I_A = \frac{240 - 224.6}{0.12} = \underline{\underline{128.3}}$$

$$\begin{aligned} R_1 &= R_{start1} - R_{start2} \\ &= 1.177 \Omega - 0.399 \Omega = \underline{\underline{0.778 \Omega}} \end{aligned}$$

$$\begin{aligned} R_2 &= R_{start2} - R_{start3} \\ &= 0.399 - 0.088 = \underline{\underline{0.311 \Omega}} \end{aligned}$$

$$R_3 = \underline{\underline{0.088 \Omega}}$$

hesaplanan I_A
değeri 185'ten küçükse
R hesabına devam

et

ex 190 ise isteme
devam et

R sayısı = 4 olur

0 zaman